

ELEVATE

A Language for Specifying Optimization Strategies

1 Wouldn't it be great...



...to **look behind the curtains** of optimizing compilers and actually understand how optimizations are applied?



...to define well-known optimizations once and **reuse** them whenever possible?



...to have **one principled way** to write compiler optimizations based on a strong theoretical foundation?



...to build your own optimizations using simple and **composable building blocks**?

Optimizing Programs like it's ~~1998~~ 2019

Visser et. al.: Building program optimizers with rewriting strategies (ICFP 1998)

2 Basic Strategy Building Blocks

A **Strategy** is a function: $Program \rightarrow Program$

A **Transformation** is the simplest strategy

e.g. `map(f) → join ∘ map(map f) ∘ split(n)`

splitJoin-Rule

id : Strategy
= $\lambda p . p$

seq : Strategy → Strategy → Strategy
= $\lambda f . \lambda s . \lambda p . s (f p)$

choice : Strategy → Strategy → Strategy
= $\lambda f . \lambda s . \lambda p . try (f p) catch (s p)$

try : Strategy → Strategy
= $\lambda s . choice s id$

repeat : Strategy → Strategy
= $\lambda s . try (s ; (repeat s))$

norm : Strategy → Strategy
= $\lambda s . repeat(find s)$

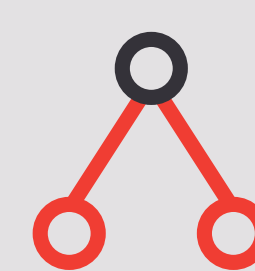
3 Traversals: Where to apply a strategy?



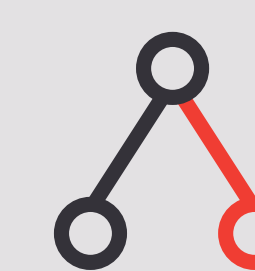
Expression

AST

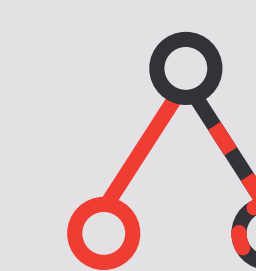
Generic one-level traversals: Strategy → Strategy



all



one



some

Generic traversal strategies: Strategy → Strategy

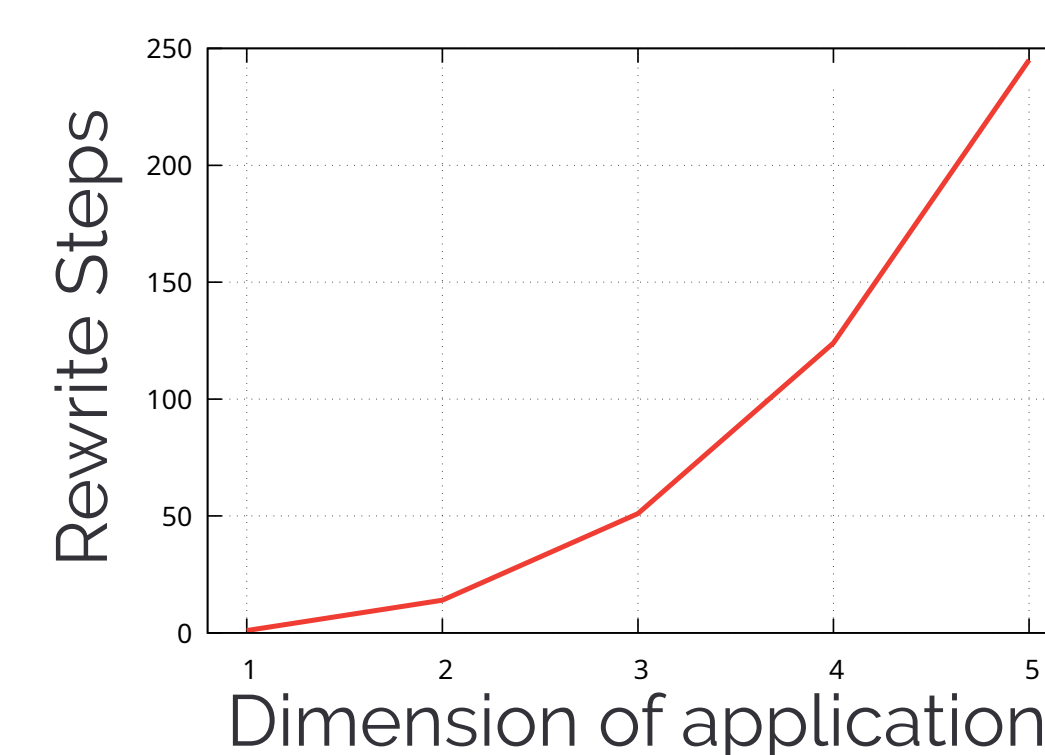
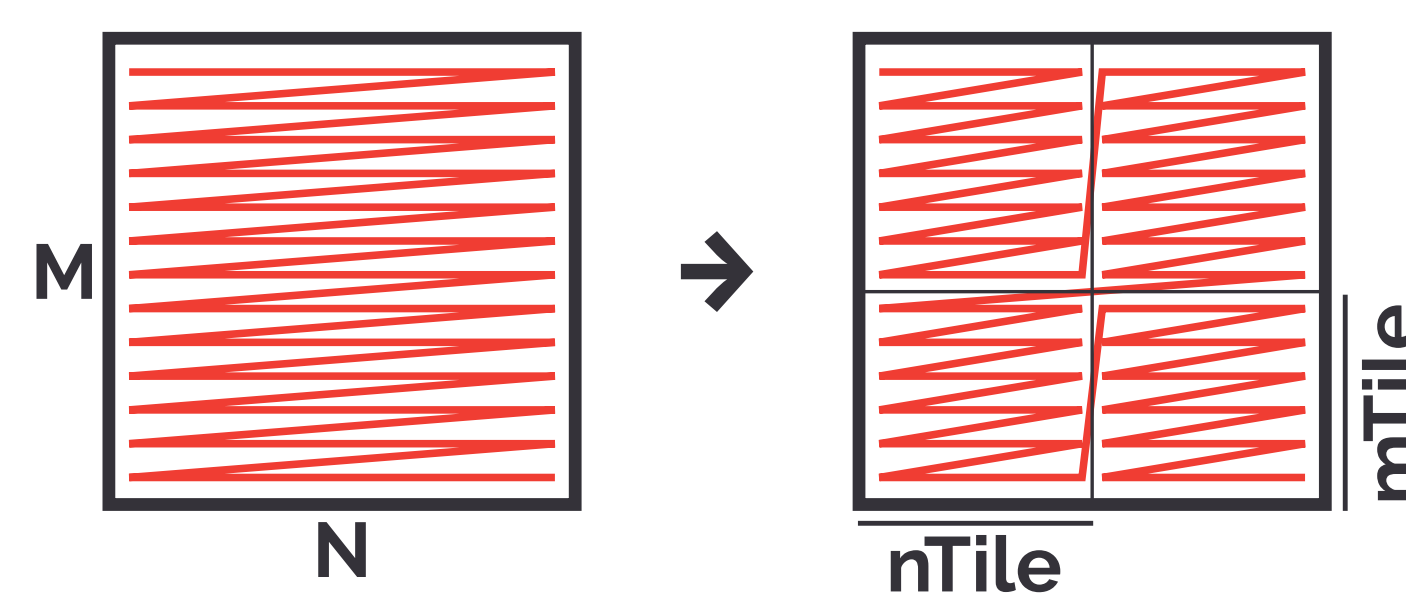
topdown = $\lambda s . s ; all (topdown s)$

tryAll = $\lambda s . all (tryAll (try s)) ; (try s)$

find = $\lambda s . s <+ one (find s)$

⋮

4 Example: Expressing tiling as a strategy in 3 simple steps...



a **Tile every dimension**
 $\lambda n . tryAll (splitJoin n)$

b **Rewrite Normalform**
norm(mapFission)
mapFission = $*(f \circ g) = *f \circ *g$

c **Rearrange dimensions**
 $\lambda d . \lambda p . d \text{ match}$
case <2 : p
case 2 : (shuffleDim d) p
case _ : (rearrangeDim (d-1) ; (shuffleDim d)) p

Example input program: ****f**

****f** → $J \circ ** (J \circ **f \circ S) \circ S$ → **Lift** (* = map | S = split(s) | J = join | T = transpose)

$J \circ ** J \circ **** f \circ ** S \circ S$ → $J \circ ** J \circ *T \circ **** f \circ *T \circ ** S \circ S$

```
for(int i = 0; i < M; i++) {
  for(int j = 0; j < N; j++) {
    // f
  }
}
```

→

```
for(int i = 0; i < M/s; i++) {
  for(int ii = 0; ii < s; ii++) {
    for(int j = 0; j < N/s; j++) {
      for(int jj = 0; jj < s; jj++) {
        // f
      }
    }
  }
}
```

→

```
for(int i = 0; i < M/s; i++) {
  for(int j = 0; j < N/s; j++) {
    for(int ii = 0; ii < s; ii++) {
      for(int jj = 0; jj < s; jj++) {
        // f
      }
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  }
}
```

OpenCL

